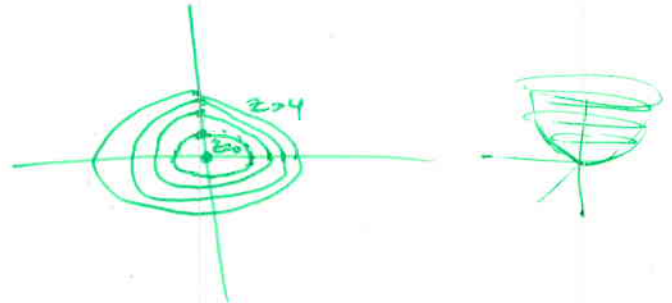


Instructions: Show all work. Use exact answers unless specifically asked to round.

1. Sketch at least 5 level curves of the graph $z = x^2 + 2y^2$. Sketch or describe the three-dimensional function based on those level curves.

$$\begin{aligned} z=0 & \quad x^2 + 2y^2 = 0 \\ z=1 & \quad x^2 + 2y^2 = 1 \\ z=2 & \quad x^2 + 2y^2 = 2 \\ z=3 & \quad x^2 + 2y^2 = 3 \\ z=4 & \quad x^2 + 2y^2 = 4 \end{aligned}$$



elliptic paraboloid

2. Find the limit, if it exists, or prove that it does not exist.

$$\lim_{(x,y) \rightarrow (0,0)} \frac{xy}{x^2 + y^3}$$

$$\begin{aligned} x^2 &= y^3 \\ x^{2/3} &= y \end{aligned}$$

$$\begin{aligned} x=0 & \\ \lim_{y \rightarrow 0} \frac{0}{y^3} &= 0 \end{aligned}$$

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$$y = kx^{2/3}$$

$$\lim_{x \rightarrow 0} \frac{x \cdot kx^{2/3}}{x^2 + (kx^{2/3})^3} = \lim_{x \rightarrow 0} \frac{x^{5/3} \cdot k}{x^2(1+k^3)} = \lim_{x \rightarrow 0} \frac{k}{x^{1/3}(1+k^3)} = \pm \infty$$

3. Find all first partial derivatives of $f(x, y, z) = xy^2 \sinh(xy) \ln(z + e^z)$.

$$\frac{\partial f}{\partial x} = \ln(z + e^z) [y^2 \sinh(xy) + xy^2 \cosh(xy) \cdot y]$$

$$\frac{\partial f}{\partial y} = \ln(z + e^z) [2xy \sinh(xy) + xy^2 \cosh(xy) \cdot x]$$

$$\frac{\partial f}{\partial z} = xy^2 \sinh(xy) \cdot \frac{1}{z + e^z} \cdot (1 + e^z)$$