

Instructions: Show all work. Answer each question as completely as possible. Use exact values. For counting problems you may use scientific notation (with three significant figures) for any numbers larger than a million.

1. What is the probability of flipped a coin ten times and getting exactly 5 heads? [Hint: it's not 50%.]

$$\binom{10}{5} \left(\frac{1}{2}\right)^{10} = .246$$

2. What is the probability of draw three-of-a-kind in a 5-card poker hand?

$$\frac{13 \binom{4}{3} \binom{48}{2}}{\binom{52}{5}} = .022569 = \frac{52 \cdot 3 \cdot 2 \cdot 48 \cdot 47}{5295}$$

3. What is the probability of rolling a sum of 4 or 6 on a pair of 6-sided dice?

$$\begin{aligned} \text{ways to get a 4} &= 3 \quad (1,3), (3,1), (2,2) \\ \text{ways to get a 6} &= 5 \quad (1,5), (5,1), (4,2), (2,4), (3,3) \\ &\frac{8}{36} = .222 \end{aligned}$$

4. What is the probability of winning a raffle with 200 tickets sold, and 4 door prizes?

$$\frac{4}{\binom{200}{4}} = 6.1838 \times 10^{-8}$$

5. What is the probability of having 3 girls in 4 children?

$$\frac{\binom{4}{3}}{16} = \frac{4}{16} = \frac{1}{4} = .25$$