

**Instructions:** Show all work. Use exact answers unless otherwise asked to round.

1. Find the eigenvalues and eigenvectors of the matrix  $A = \begin{bmatrix} -4 & -1 \\ 6 & 1 \end{bmatrix}$ . Is the matrix diagonalizable? Why or why not?

$$(-4-\lambda)(1-\lambda)+6=0$$

$$\lambda^2+3\lambda+2=0$$

$$(\lambda+2)(\lambda+1)=0$$

$$\lambda = -2, -1$$

$$\lambda = -2 \quad \begin{bmatrix} -2 & -1 \\ 6 & 3 \end{bmatrix} \quad \begin{array}{l} 6x_1 = -3x_2 \\ x_1 = -\frac{1}{2}x_2 \end{array} \quad \begin{bmatrix} -1 \\ 2 \end{bmatrix}$$

$$\lambda = -1 \quad \begin{bmatrix} -3 & -1 \\ 6 & 2 \end{bmatrix} \quad \begin{array}{l} 6x_1 = 2x_2 \\ x_1 = \frac{1}{3}x_2 \end{array} \quad \begin{bmatrix} -1 \\ 3 \end{bmatrix}$$

yes, it is diagonalizable  
there are distinct  
eigenvalues

2. Find the eigenvalues and eigenvectors of the matrix  $A = \begin{bmatrix} 5 & 3 \\ -4 & 4 \end{bmatrix}$ . If the eigenpairs are real, what size space do they span?

$$(5-\lambda)(4-\lambda)+12=0$$

$$\lambda^2-9\lambda+32=0$$

$$\lambda = \frac{9 \pm \sqrt{81-128}}{2} =$$

$$\lambda = \frac{9}{2} \pm \frac{\sqrt{47}}{2}i$$

the eigenvalues are  
not real