

Instructions: Show all work. Use exact answers unless otherwise asked to round.

1. Find a basis for the space spanned by the vectors $\left\{ \begin{bmatrix} 9 \\ 3 \\ 2 \\ 1 \end{bmatrix}, \begin{bmatrix} -1 \\ 4 \\ 2 \\ -3 \end{bmatrix}, \begin{bmatrix} 0 \\ 1 \\ 1 \\ -1 \end{bmatrix}, \begin{bmatrix} 7 \\ 5 \\ 3 \\ 2 \end{bmatrix} \right\}$.

2. Given the basis $\{2 - t, t + t^2, 3t^2 - t^3, 1 + 4t^3\}$ for P_3 , find the representation of $p(t) = 5t^2 - 3t + 17$ in this basis. Clearly label your change of basis matrix and correct notation for each vector used.