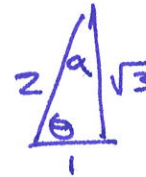


**Instructions:** Show all work. Give exact answers unless specifically asked to round.

1. Solve the equation for all angles in  $[0, 2\pi)$ .

a.  $\tan 3x = \frac{\sqrt{3}}{3} = \frac{1}{\sqrt{3}}$

$$\tan \alpha = \frac{1}{\sqrt{3}} \quad \alpha = \frac{\pi}{6}, \frac{7\pi}{6}$$



$$3x = \frac{\pi}{6}$$

$$x = \frac{\pi}{18}, \frac{7\pi}{18}, \frac{13\pi}{18}, \frac{19\pi}{18}, \frac{25\pi}{18}, \frac{31\pi}{18}$$

- b.  $4 \sin^2 x + 4 \cos x - 5 = 0$

$$4(1 - \cos^2 x) + 4 \cos x - 5 = 0$$

$$4 - 4 \cos^2 x + 4 \cos x - 5 = 0$$

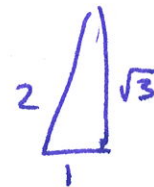
$$4 \cos^2 x - 4 \cos x + 1 = 0$$

$$(2 \cos x - 1)^2 = 0$$

$$2 \cos x - 1 = 0$$

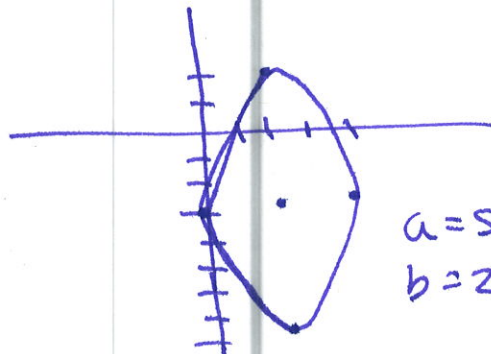
$$\cos x = \frac{1}{2}$$

$$x = \frac{\pi}{3}, \frac{5\pi}{3}$$



2. Sketch the graph of the ellipse with a center at  $(2, -3)$  and one endpoint of the major axis at  $(2, 2)$ , and one endpoint of the minor axis at  $(4, -3)$ . Write the equation in standard form.

$$\frac{(x-2)^2}{4} + \frac{(y+3)^2}{25} = 1$$



$$a = 5$$

$$b = 2$$