

Instructions: Show all work, and provide exact answers. For full credit will be given to the steps shown than for the final answer. Be sure to provide thorough explanations.

1. Integrate.

$$\begin{aligned} \text{a. } \int \frac{5}{\sqrt[4]{x^7}} dx &= \int 5x^{-7/4} dx = 5\left(\frac{4}{-3}\right)x^{-3/4} + C \\ &= -\frac{20}{3}x^{-3/4} + C = \frac{-20}{3\sqrt[4]{x^3}} + C \end{aligned}$$

b. $\int 3e^{4x} dx$

$$= \frac{3}{4}e^{4x} + C$$

2. Evaluate $\sum_{i=1}^6 (5i + i^2)$

$$\begin{aligned} &(5+1) + (10+4) + (15+9) + (20+16) + (25+25) + (30+36) \\ &= 6 + 14 + 24 + 36 + 50 + 66 = 196 \end{aligned}$$

3. Find the area under the curve $y = x^3$ on the interval $[0,2]$. Sketch the graph.

$$\begin{aligned} \int_0^2 x^3 dx &= \\ \frac{1}{4}x^4 \Big|_0^2 &= \\ \frac{1}{4}[2^4 - 0] &= \frac{1}{4}[16] \\ &= 4 \end{aligned}$$

