

Instructions: This exam is in three parts: Part I is to be completed partly at home using the materials posted on Blackboard for Part I and you will answer questions about that work in class below; Part II is to be completed entirely in class using your computer. Part III is to be done entirely in class without your computer.

1. You may not use cell phones, and you may only access internet resources you are specifically directed to use: You may access your data file for Part I of the exam in Blackboard. You may access the data files posted to Blackboard for the Exam part II, but not for Part III.
2. It is a violation of the honor code to communicate with other students in or out of the class during the exam, by any means. Students whose exams show evidence of coordination will be reported.
3. Show all work to support your reasoning. Primarily, this can be done in Excel. Deletion of evidence of your logical process can result in loss of credit. A significant amount of credit goes toward process, reasoning and interpretation.
4. When rounding, do not over-round. In general, do not report dollar amounts beyond the penny. Means should be rounded to one digit more than the original data; standard deviations to two digits more. Do not report fractions rounded to single digit expressions: $\frac{131}{256} \neq \frac{1}{2}$, and do not round decimals or percents to a single digit: $0.57846 \dots \neq 60\%$ or 0.6 . Report a minimum of two digits, up to four, unless otherwise specified in the problem.
5. If a problem asks for an explanation, state the solution clearly, then interpret or explain in addition to stating the solution, not in place of. Explanations without solutions, just as solutions without explanations, will not be awarded full credit.

Part I: At Home

This part was completed at home. You can upload the Excel file for Part I to the Part I folder in Blackboard for use during the Exam period. However, this submission will **not** be graded in this location, it must be submitted to the “**to be graded** folder” to receive credit.

Part II: In Class (with computer)

Before completing Part III, complete Part II in class. Return the paper to your instructor and put away your computer. Then pick up Part III.

Part III: In Class (without computer)

1. You may use a handheld calculator for this portion of the exam. Any calculator is fine, as long as it is not on a device that connects to the Internet. That means, you may not use the calculator on your phone or smart watch. You may also not share calculators with another student taking the exam at the same time.
2. This is Exam E.
3. Answer the questions on the paper exam. Sign the honor code statement on the next page.
4. Turn in your paper copy of the exam to your instructor. Your instructor will attach this portion of the exam to the version of Part II that you submitted previously.

Honor Code Statement:

I, _____ (print your name), agree to abide by the George Mason Honor Code and Academic Integrity Pledge: *To promote a stronger sense of mutual responsibility, respect, trust, and fairness among all members of the George Mason University Community and with the desire for greater academic and personal achievement, I, a student member of the university community, pledge not to cheat, plagiarize, steal, or lie in matters related to academic work.* Furthermore, I have read and I agree to follow the guidelines laid out in the instructions for this exam above. I also agree not to participate in the efforts of other students to circumvent these guidelines, or to assist in their violations of the code, and will report such efforts in a timely manner.

Student Signature and G#

Today's Date

Part III:

Below you will find screenshots of the set-up for a linear programming problem on planting. Use this information to answer the questions that follow.

| | A | B | C | D | E | F | G | H | I | J | K | L | M |
|----|---------|----------|----------|----------|------------|----------------|---|---|---|---|---|---|---|
| 1 | | Oats | Corn | Total | Inequality | Available/Goal | | | | | | | |
| 2 | Acres | 83.33333 | 16.66667 | 100 | <= | 100 | | | | | | | |
| 3 | | | | | | | | | | | | | |
| 4 | Capital | 18 | 36 | 2100 | <= | 2100 | | | | | | | |
| 5 | Labor | 2 | 6 | 2133.333 | <= | 2400 | | | | | | | |
| 6 | | | | | | | | | | | | | |
| 7 | Revenue | 55 | 125 | 6666.667 | | | | | | | | | |
| 8 | | | | | | | | | | | | | |
| 9 | Profit | 6933.333 | | | | | | | | | | | |
| 10 | | | | | | | | | | | | | |

A farmer has 100 acres on which to plant oats or corn. Each acre of oats requires \$18 capital and 2 hours of labor. Each acre of corn requires \$36 capital and 6 hours of labor. Labor costs are \$8 per hour. The farmer has \$2100 available for capital and \$2400 for labor. If the revenue is \$55 from each acre of oats and \$125 from each acre of corn, what planting combination will produce the greatest total profit? What is the maximum profit (revenue+leftover cash reserve +labor cash reserve)?

| Variable Cells | | | | | | |
|----------------|------------|-------------|--------------|-----------------------|--------------------|--------------------|
| Cell | Name | Final Value | Reduced Cost | Objective Coefficient | Allowable Increase | Allowable Decrease |
| \$B\$2 | Acres Oats | 83.33333333 | 0 | 21 | 20 | 0.5 |
| \$C\$2 | Acres Corn | 16.66666667 | 0 | 41 | 1 | 20 |

| Constraints | | | | | | |
|-------------|---------------|-------------|--------------|----------------------|--------------------|--------------------|
| Cell | Name | Final Value | Shadow Price | Constraint R.H. Side | Allowable Increase | Allowable Decrease |
| \$D\$2 | Acres Total | 100 | 1 | 100 | 16.66666667 | 16.66666667 |
| \$D\$4 | Capital Total | 2100 | 1.111111111 | 2100 | 150 | 300 |
| \$D\$5 | Labor Total | 2133.333333 | 0 | 2400 | 1E+30 | 266.6666667 |

Solver Parameters

Set Objective: ↑

To: Max Min Value Of:

By Changing Variable Cells: ↑

Subject to the Constraints:

\$D\$2 <= \$F\$2

\$D\$4 <= \$F\$4

\$D\$5 <= \$F\$5

Make Unconstrained Variables Non-Negative

Select a Solving Method: Options

1. What is the final maximum profit for planting 83.3 acres of oats, and 16.7 acres of corn? (4 points)

2. What is the shadow price for the Capital constraint? What does it mean in the context of the problem? (6 points)

3. What does it mean for a linear programming problem to be infeasible? (6 points)

Below you will find a screenshot of the relevant Excel data for a difference of means problem. Use this information to answer the questions that follow.

| | A | B | C | D |
|----|----------|------------------|------------|---------------------------|
| 1 | Pair | Male | Female | Difference: Male - Female |
| 41 | 40 | \$29,752 | \$29,188 | \$564 |
| 42 | 41 | \$30,414 | \$30,095 | \$319 |
| 43 | 42 | \$25,795 | \$25,248 | \$547 |
| 44 | 43 | \$27,944 | \$27,673 | \$271 |
| 45 | 44 | \$26,661 | \$26,212 | \$449 |
| 46 | 45 | \$31,351 | \$30,783 | \$568 |
| 47 | 46 | \$29,303 | \$28,519 | \$784 |
| 48 | 47 | \$28,628 | \$28,644 | -\$16 |
| 49 | 48 | \$24,524 | \$24,114 | \$410 |
| 50 | 49 | \$27,217 | \$26,282 | \$935 |
| 51 | 50 | \$21,651 | \$21,153 | \$498 |
| 52 | Mean | \$27,241 | \$26,944 | \$297 |
| 53 | St.Dev. | \$2,536.45 | \$2,548.50 | \$ 297.87 |
| 54 | | | | |
| 55 | T-Score | Confidence Level | | Standard Error |
| 56 | 2.009575 | 95% | | \$ 42.13 |
| 57 | | | | |

4. Is the data dependent or independent? Explain what leads you to this conclusion. (6 points)

5. Use the information provided to calculate the 95% confidence interval. (6 points)

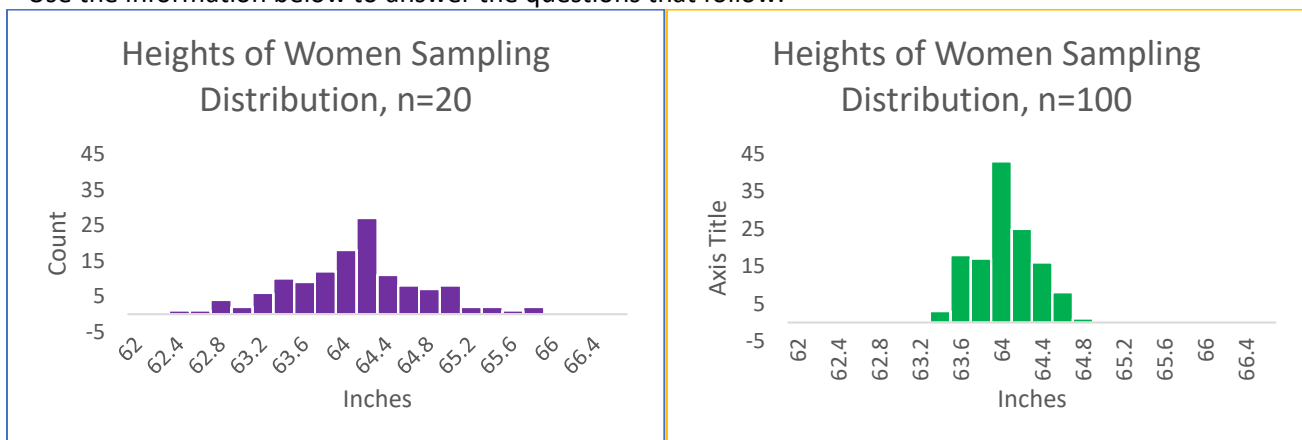
6. Does the interval you calculated support the claim that men make more than women? Why or why not? (6 points)

Use the data in the table below to answer the questions that follow.

| Preference | Count | Proportion |
|------------|-------------------|------------|
| R | 181 | 45.25% |
| N | 29 | 7.25% |
| L | 190 | 47.50% |
| | | |
| Z-Scores | Confidence Levels | |
| 1.150 | 75% | |
| 1.282 | 80% | |
| 1.645 | 90% | |
| 1.960 | 95% | |
| 2.576 | 99% | |

- Use the data provided to find the margin of error for the 90% confidence interval for those that prefer N. (5 points)
- Use the data provided to find the margin of error for the 99% confidence interval for those that prefer N. (5 points)
- What do you notice about the margin of error as the confidence level increases? (5 points)

Use the information below to answer the questions that follow.



| Sample Size | Standard Error | Mean |
|--------------------|-----------------------|-------------|
| <i>n=20</i> | 0.6658 | 64.05 |
| <i>n=100</i> | 0.2924 | 64.03 |
| <i>n=1</i> | 3.1 | 64 |

10. Explain how the information above supports the claims of the Central Limit Theorem. Be as thorough as possible. (6 points)

11. Describe a scenario in which a systematic sample would be a more appropriate choice than a simple random sample. (6 points)

12. What is a measurement error? How does it produce excess bias in a sample? (6 points)

13. Why does confidentiality reduce untruthful responses? (5 points)

14. What conditions should be met to substitute a z-score in a confidence interval for means instead of a t-score? (6 points)

15. Write the Excel formula to find t-score for an 92% confidence interval. (5 points)

16. What assumptions are made when using a two-sample pooled t-confidence interval? (4 points)

Standard errors: $\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$ $\sigma_{\hat{p}} = \sqrt{\frac{p(1-p)}{n}}$ $S_{pooled} = \sqrt{\frac{(n_1-1)s_1^2 + (n_2-1)s_2^2}{n_1+n_2-2}}$

$$S_{x_1-x_2} = S_{pooled} \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$$

Sample sizes: $n > \hat{p}(1-\hat{p}) \left(\frac{z_{\alpha/2}}{E}\right)^2$ $n > \left(\frac{z_{\alpha/2}\sigma}{E}\right)^2$ $m = n = \frac{4z_{\alpha/2}^2(\sigma_1^2 + \sigma_2^2)}{w^2}$

Confidence intervals:

One sample: $\bar{x} \pm t_{\alpha/2, n-1} \frac{s}{\sqrt{n}}$ $\hat{p} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$

Two samples (independent): $(\bar{x}_1 - \bar{x}_2) \pm t_{\alpha/2, n-1} \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$ $(\hat{p}_1 - \hat{p}_2) \pm z_{\alpha/2} \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}}$