BUS 310, Fi	inal Exam	F, Part	III,	Spring	2019
-------------	-----------	---------	------	--------	------

Name	KEY	100
Section		

**Instructions**: This exam is in three parts: Part I is to be completed partly at home using the materials posted on Blackboard for Part I and you will answer questions about that work in class below; Part II is to be completed entirely in class using your computer. Part III is to be done entirely in class without your computer.

- 1. You may not use cell phones, and you may only access internet resources you are specifically directed to use: You may access your data file for Part I of the exam in Blackboard. You may access the data files posted to Blackboard for the Exam part II, but not for Part III.
- 2. It is a violation of the honor code to communicate with other students in or out of the class during the exam, by any means. Students whose exams show evidence of coordination will be reported.
- 3. Show all work to support your reasoning. Primarily, this can be done in Excel. Deletion of evidence of your logical process can result in loss of credit. A significant amount of credit goes toward process, reasoning and interpretation.
- 4. When rounding, do not over-round. In general, do not report dollar amounts beyond the penny. Means should be rounded to one digit more than the original data; standard deviations to two digits more. Do not report fractions rounded to single digit expressions:  $\frac{131}{256} \neq \frac{1}{2}$ , and do not round decimals or percents to a single digit:  $0.57846 \dots \neq 60\%$  or 0.6. Report a minimum of two digits, up to four, unless otherwise specified in the problem.
- 5. If a problem asks for an explanation, state the solution clearly, then interpret or explain in addition to stating the solution, not in place of. Explanations without solutions, just as solutions without explanations, will not be awarded full credit.

## Part I: At Home

This part was completed at home. You can upload the Excel file for Part I to the Part I folder in Blackboard for use during the Exam period. However, this submission will not be graded in this location, it must be submitted to the "to be graded folder" to receive credit.

Part II: In Class (with computer)

Before completing Part III, complete Part II in class. Return the paper to your instructor and put away your computer. Then pick up Part III.

Part III: In Class (without computer)

- 1. You may use a handheld calculator for this portion of the exam. Any calculator is fine, as long as it is not on a device that connects to the Internet. That means, you may not use the calculator on your phone or smart watch. You may also not share calculators with another student taking the exam at the same time.
- 2. This is Exam F.
- 3. Answer the questions on the paper exam. Sign the honor code statement on the next page.
- 4. Turn in your paper copy of the exam to your instructor. Your instructor will attach this portion of the exam to the version of Part II that you submitted previously.

Honor Code Statement:			•
respect, trust, and fairnes desire for greater academ pledge not to cheat, plagi	is among all members of ic and personal achiever arize, steal, or lie in mati the guidelines laid out i ts of other students to ci	e: To promote a stronger the George Mason Univer ment, I, a student member ters related to academic in the instructions for this rcumvent these guideling	ree to abide by the George sense of mutual responsibility, ersity Community and with the er of the university community, work. Furthermore, I have s exam above. I also agree not es, or to assist in their
Student Signature and G#			Today's Date

## Part III:

1. When a hypothesis test is conducted, there are four possible combinations of outcomes: The null can be true, the null can be false, our conclusion can agree with the true state of nature, or it may not. A table of these situations is shown below. Two of these combinations are correct and two produce errors. Label all four possibilities as correct, or, if an error, which kind of error it is. (4 points)

Nature: Ho True

Correct

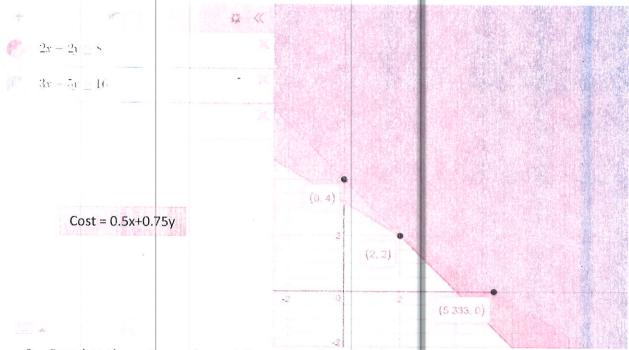
Type I

Correct

Correct

Correct

Below you will find the Desmos plot for the constraints for a linear programming problem. The graph shows the feasible region and its cornerpoints, the constraints graphed, and the cost function to be minimized. Not shown are the non-negativity constraints. Use this information to answer the questions that follow.



2. Based on the cost equation and the cornerpoints, find the minimum cost, and the values of the two variables produce this cost. (8 points)

0.5(6) + 0.75(4) = 3 0.5(2) + 0.75(2) = 3.5 minimum ( (2,2) 0.5(5.333) + 0.75(6) = 3.66 Below you will find a boxplot and output for a two-sample t-test of two brands of light bulbs. Use this information to answer the questions that follow.

t-Test: Paired Two Sample for

Means

P(T<=t) one-tail

t Critical one-tail

P(T<=t) two-tail

t Critical two-tail

	Variable 1	Variable 2
Mean	100.0898	99.5594
Variance	7.958329253	39.76949661
Observations	100	100
Pearson Correlation	-0.120363277	
Hypothesized Mean		
Difference	0	
df	99	
t Stat	0.735458562	
P(T<=t) one-tail	0.231899543	
t Critical one-tail	1.660391156	
P(T<=t) two-tail	0.463799087	
t Critical two-tail	1.984216952	
t-Test: Two-Sample Assuming Equal Variances		,
	Variable 1	Variable 2
Mean	100.0898	99.5594
Variance	7.958329253	39.76949661
Observations	100	100
Pooled Variance	23.86391293	
Hypothesized Mean		
Difference	0	
df	198	
t Stat	0.767746225	

	A	В	C	D
1	Brai	nd 2	Bran	nd 2
2	Battery	Lifetime	Battery	Lifetime
S	1	99.11	1	110.65
4 5	2	99.45	2	92.24
	3	98.39	3	96.63
6	4	97.07	4	99.45
7	5	99.97	5	102.55
8	6	100.06	6	109.60
9	7	98.20	7	96.53
10	8	98.13	8	104.64
11	9	107.73	9	88.03
12	10	95.58	10	96.87
13	11	96.98	11	96.02
14	12	100.47	12	97.33
15	13	101.23	13	105.14
16	14	100.39	14	99.86
17	15	106.07	15	93.81
18	16	98.02	16	92.26
19	17	100.26	17	103.67
20	18	102.48	18	93.61
21	19	97.88	19	97.28
**	~~~			

3. Based on the snapshot of the data, would you conclude that that the lightbulb data collected for the two brands are dependent or independent? (4 points)

0.221776286

1.652585784

0.443552573

1.972017478

independent

4. Based on your decision above, should you use the paired two-sample t-test, or the pooled (equal variance) two-sample t-test? (4 points)

pooled equal vanance

5. If the company wants to know whether Brand 2 has a shorter lifespan than Brand 1, does that correspond to a one-tailed or two-tailed t-test (4 points)

1 - failed

6. State the null and alternative hypotheses, the test-statistic and p-value for the test described in the previous questions. State your conclusion in language a person not familiar with statistics can understand. (8 points)

Ho: M1 = M2 Ha: M1 ≠ M2

t= 0.7677

p-value = 0.44 >0.05

There is not sufficient enderie to think mean difetimes are different

fail to nglet null
Use the data in the correlation table to answer the question that follows.

	Three- month	Six-month	One-year	Five-year	Seven-year	Ten-year	Thirty- year
Three- month	1						
Six-month	0.995018236	1		e to care Anni Caren Vitoriti e tra i Albania i Care Area anni		· · · · · · · · · · · · · · · · · · ·	
One-year	0.980587641	0.994322863	1				
Five-year	0.824150317	0.861942602	0.896782787	1			
Seven-year	0.764325584	0.806788198	0.847048391	0.993284711	- /		
Ten-year	0.708407903	0.754748746	0.799680553	0.979556259	0.995836885	1	
Thirty-year	0.581770384	0.631833095	0.682138948	0.925093011	0.960802599	0.980922012	1

7. Based on the correlation table, which variable appears to be the best predictor of 10-year market averages? Explain your reasoning. (5 points)

7-year market averages highest Cornelation value

8. Why does it appear that the highest correlations for each variable on just off the diagonal? Why does this make sense in the real world? (6 points)

it means the most recent behaviour is The best predictor. This makes sense

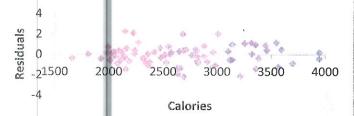
Use the data in the residual graphs, scatterplots, and regression output on the pages that follow to answer the remaining questions. Included elements are a snapshot sample of all available variables used in the complete model (the first regression output). Two more regression outputs are included: Calories vs. GNP per Capita as a linear model, and Calories vs. LN(GNP per Capital) which analyses the exponential model shown in the scatterplot. The residual plots correspond to the linear and log models for the last two regression outputs respectively.

	А	В	С	D	E	F
1	Country	GNP per Capita	Population Growth	Calories	Life Expectancy	Fertility
2	Antigua_&_Barbud	4595	0,5%	2222	74	1.9
3	Argentina	2369	1.4%	3118	71	2.8
4	Bahamas	11514	1.9%	2678	69	2.2
5	Bangladesh	199	2.6%	1925	52	4.8
6	Belgium	15444	0.1%	3942	76	1.6
7	Belieze	1974	2.8%	2649	68	4.7
8	Benin	362	3.2%	2145	51	6.3
9	Boliva	619	2.8%	2086	54	5.9

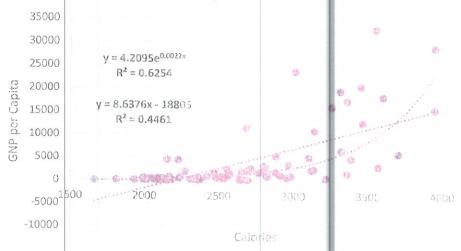
## **Calories Residual Plot**

40000

## Calories (log) Residual Plot







9. Based on the first model containing all the variables, conduct a hypothesis test on the coefficient for Calories. State the null and alternative hypotheses, test-statistic and p-value. Does this test explain why the variable was kept in the final model? (8 points)

this does explain why its in the final model because the p-value is extremely low

10. Using the scatterplot, does the data appear to be linear or non-linear? (4 points)

The data appears to be lettier norbinear or possibly unequal variance

the residual plot suggests non-linear is more likely

11. Model 2 is the linear model, and Model 3 the non-linear model. In which model is the  $R^2$  value higher? State the higher value. Does this confirm your answer from above? (4 points)

Model 3 higher R2=0.625

Yes.

12. In the third Model, what is the proportion of variability in GNP per capita can be explained by the relationship with Calories? (4 points)

62.5%

13. Use Model 2 to predict the GNP for capita of a country with a population growth rate of 1.5%, consumes 1500 calories per day, has a life expectancy of 68 years and a fertility rate of 5.6. If the variable does not appear in the model, ignore it. (6 points)

$$Y = 8.638 \times -18,805$$

$$= -5848$$

14. Construct a 95% prediction interval for the prediction above. You may use 1.96 as the multiplier for the prediction margin. (6 points)

margin of error/prediction 1.96 \* 5174.6 = 10,142.2

15. Report the 99% confidence interval for the Population Growth coefficient from Model 1 (the full model). (4 points)

(-353,332.4, 142,775,7)

# SUMMARY OUTPUT (model 1)

tics	0.691027162	0.477518538	0.44965286	5125.104196	80	
Regression Statistics	Multiple R	R Square	Adjusted R Square	Standard Error	Observations	ANOVA

						Upper 99.0%	14526.73642	2. 0. 1. 1.	142775.7296 10.47705469		443.6148342 2648.910285
					700 00 50000	Lower 33.0% Upper 99.0%	-466/8.35565 14526.73642	-292244 7645 81688 06288 25222 COCK CCCCC	1.544708177 10.47705469	C 100 11	0.9130213 -1811.603959 2022.543466 -2437.970778 2648.910285
Significance	5.0615F-10				11mor 050/	- 1	0990.322983	81688 06388	9.377181233	-172 0589558 357 1589657	2022.543466
Т.	17.13644071				10MPr 95%	-301/1 0/224	77747.74767	-2927 44 7645	2.644581635	-172 0589558	-1811.603959
MS	1800470511 450117627.7 17.13644071	26266693.02			P-value	0 169130089		0.265557203	0.000653986	0.696760471 0.488106706	0.9130213
SS	1800470511	1970001977	3770472487		t Stat	-1.388384739 0 169130089		-1.121726751 0.265557203	3.557107379 0.000653986	0.696760471	0.109597519
df	4	75	79	Standard	Error	11578.79005		93853.82864	1.68982288	132.8290119	962.3370513
					Coefficients	-16075.80961		-105278.3503	6.010881434	92.55000493	105.4697533
	Regression	Residual	Total			Intercept	Population	Growth	Calories Life	Expectancy	Fertility

## SUMMARY OUTPUT (model 2)

neylession statistics	lalistics
Multiple R	0.66789146
R Square	0.446079002
Adjusted R Square	0.438977451
Standard Error	5174.572795
Observations	08

ANOVA

						Unner 99.0%	-11016.44917	11.51514307
						P-value Lower 95% Upper 95% Lower 99.0%	-26593.45382	5.76003868
Significance	ч.	1681928606 1.68E+09 62.8143 1.31146E-11				Upper 95%	1.19E-08 -24677.5728 -12932.33019 -26593.45382	1.31E-11 6.467883064 10.80729868
	Ā	62.8143				wer 95%	677.5728	7883064
	MS	1.68E+09	2088543882 26776204			107 ar	-08 -24	-11 6.46
		58606	13882	72487		P-valu	1	1.31E
	SS	168192	208854	3770472487		t Stat	-6.37497	
	df	T	78	79	Standard	Error	2949.810357 -6.37497	8.637590872 1.089841526 7.925548
						Coefficients	-18804.95149	8.637590872
		Regression	Residual	Total			Intercept	Calories

SUMMARY OUTPUT (model 3)

Regression Statistics	Statistics
Multiple R	0.79081175
R Square	0.625383224
Adjusted R	
Square	0.620580445
Standard Error	0.90822106
Observations	80
ANOVA	

					-	%0	077	823
						Upper 99	2.8043480	0.002687
						Upper 95% Lower 99,0% Upper 99,0%	0.517739337 2.77618501 0.006883209 0.406600345 2.46808003 0.070332298 2.804348077	0.000191285 11.41108141 2.64932E-18 0.001801947 0.002563585 0.001677709 0.002687823
						Upper 95%	2.46808003	0.002563585
Significance	F	2.64932E-18				Lower 95%	0.406600345	0.001801947
	1	130.2127789				P-value	0.006883209	2.64932E-18
	MS	107.4080282 107.4080282 130.2127789 2.64932E-18	0.824865494			t Stat	2.77618501	11.41108141
	SS	107.4080282	64.33950854 0.824865494	171.7475367	Standard	Error	0.517739337	0.000191285
	df	Н	78	79		Coefficients	1.437340187	0.002182766
		Regression	Residual	Total			Intercept	Calories

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

$$\sigma_{\hat{p}} = \sqrt{\frac{p(1-p)}{n}}$$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$
  $\sigma_{\hat{p}} = \sqrt{\frac{p(1-p)}{n}}$   $s_{pooled} = \sqrt{\frac{(n_1-1)s_1^2 + (n_2-1)s_2^2}{n_1 + n_2 - 2}}$ 

$$S_{x_1 - x_2} = S_{pooled} \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$$

**Sample sizes**: 
$$n > \hat{p}(1 - \hat{p}) \left(\frac{z_{\alpha/2}}{E}\right)^2$$
  $n > \left(\frac{z_{\alpha/2}\sigma}{E}\right)^2$   $m = n = \frac{4z_{\alpha/2}^2(\sigma_1^2 + \sigma_2^2)}{w^2}$ 

$$n > \left(\frac{z_{\alpha/2}\sigma}{R}\right)^2$$

$$m = n = \frac{4z_{\alpha/2}^2(\sigma_1^2 + \sigma_2^2)}{w^2}$$

## Confidence intervals:

$$\bar{x} \pm t_{\alpha/2,n-1} \frac{s}{\sqrt{n}}$$

$$\hat{p} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

Two samples (independent): 
$$(\bar{x}_1 - \bar{x}_2) \pm t_{\alpha/2, n-1} \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$
  $(\hat{p}_1 - \hat{p}_2) - z_{\alpha/2} \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}}$ 

$$(\hat{p}_1 - \hat{p}_2) - z_{\alpha/2} \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}}$$

## Test statistics:

One sample: 
$$z \text{ or } t = \frac{\bar{x} + \mu_0}{s / \sqrt{n}}$$

$$z = \frac{\hat{p} - p_0}{\sqrt{p_0(1 - p_0)/n}}$$

Two samples: dependent: 
$$z$$
 or  $t = \frac{\overline{d}_0 - \delta}{\frac{S_d}{\sqrt{n}}}$ 

Independent: 
$$z \text{ or } t = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

$$Z = \frac{(\hat{p}_1 - \hat{p}_2) - (p_1 - p_2)}{\sqrt{\frac{p_1(1 - p_1)}{n_1} + \frac{p_2(1 - p_2)}{n_2}}}$$

Degrees of freedom (two samples, unpooled) 
$$v = \frac{\left(\frac{s_1^2}{n}, \frac{s_2^2}{n}\right)^2}{\frac{\left(\frac{s_1^2}{n}\right)^2}{m-1}, \frac{\left(\frac{s_2^2}{n}\right)^2}{n-1}}$$

$$\nu = \frac{\left(\frac{s_1}{m} + \frac{s_2}{n}\right)}{\frac{\left(\frac{s_1^2}{m}\right)^2}{m-1} + \frac{\left(\frac{s_2^2}{n}\right)^2}{n-1}}$$

$$\chi^2$$
Tests:

$$\chi^2$$
Tests:  $\chi^2 = \sum_{all\ cells} \frac{(obs - \exp)^2}{exp}$ 

ANOVA: 
$$MSE = \frac{\left(\sum_{j=1}^{J} n_{j} (\bar{Y}_{j} - \bar{Y})^{2}\right)}{J-1}$$
  $MSS = \sum_{j=1}^{J} \frac{(n_{j}-1)s_{j}^{2}}{n-J}$ 

$$MSS = \sum_{j=1}^{J} \frac{(n_j - 1)s_j^2}{n - J}$$

$$F = \frac{MSE}{MSS}$$