

Instructions: Show all work. Answers without work required to obtain the solution will not receive full credit. Some questions may contain multiple parts: be sure to answer all of them. Give exact answers unless specifically asked to estimate.

1. A spring-mass system stretches 6 cm when a 3N force is applied. A viscous damper is attached that applies a force of 2N when the velocity is 5 cm/sec. A 10 kg mass is hung from the spring and is set in motion from equilibrium with an initial velocity upward of 1 cm/sec. Set up the second order ODE that describes the motion.

$$F = kx$$

$$3 = k(.06)$$

$$k = 50$$

$$\gamma v = F$$

$$\gamma(.05) = 2$$

$$\gamma = 40$$

$$m = 10 \text{ kg}$$

$$y(0) = 0$$

$$y'(0) = .01$$

$$10y'' + 40y' + 50y = 0$$

$$y(0) = 0, y'(0) = .01$$

$$\text{or } y'' + 4y' + 5y = 0$$