

Instructions: Show all work. Use exact answers unless otherwise asked to round.

1. Evaluate the integral $\int_0^1 \int_x^1 e^{x/y} dy dx$ by reversing the order of integration.

2. Set up and evaluate $\iiint_Q x dV$ where Q is bounded by the cylinder $y^2 + z^2 = 9$ and the planes $x = 0, y = 3x, z = 0$ in the first octant. Use an appropriate coordinate system.

3. Set up and evaluate $\iiint_Q x e^{x^2+y^2+z^2} dV$ where Q is the portion of the unit ball $x^2 + y^2 + z^2 \leq 1$ that lies in the first octant. Use an appropriate coordinate system.

4. Consider the space curve $\vec{r}(t) = t\hat{i} + e^t\hat{j} + e^{-t}\hat{k}$.
- Find $\vec{r}'(t)$
 - Find $\|\vec{r}'(t)\|$.
 - Are there any points at which $\|\vec{r}'(t)\|$ reaches an extremum? (minimum or maximum?)
 - Find the unit tangent vector $\vec{T}(t)$.
5. Find the unit normal vector of $\vec{r}(t) = \cos 4t\hat{i} + t\hat{j} - \sin 4t\hat{k}$.
6. Find the directional derivative for the function $f(x, y) = x^2y - e^{x-y}$ at the point $(1, 1)$ in the direction of $\langle 2, -5 \rangle$.